

WHY

Population genetics and Hardy-Weinberg matter

Hardy-Weinberg:
 $p = f(A)$
 $q = f(a)$

$$p^2 + 2pq + q^2 = 1$$


Evolution

In one of the last classes we have covered:

What is the evidence for evolution?

Darwin observations

Evolution

In this class we will cover:

- The Hardy-Weinberg Equilibrium
- Hardy-Weinberg and its assumptions
- Each assumption is a population genetic process
- How to evaluate the HWE in a sample
- What are the main factors that affect HWE

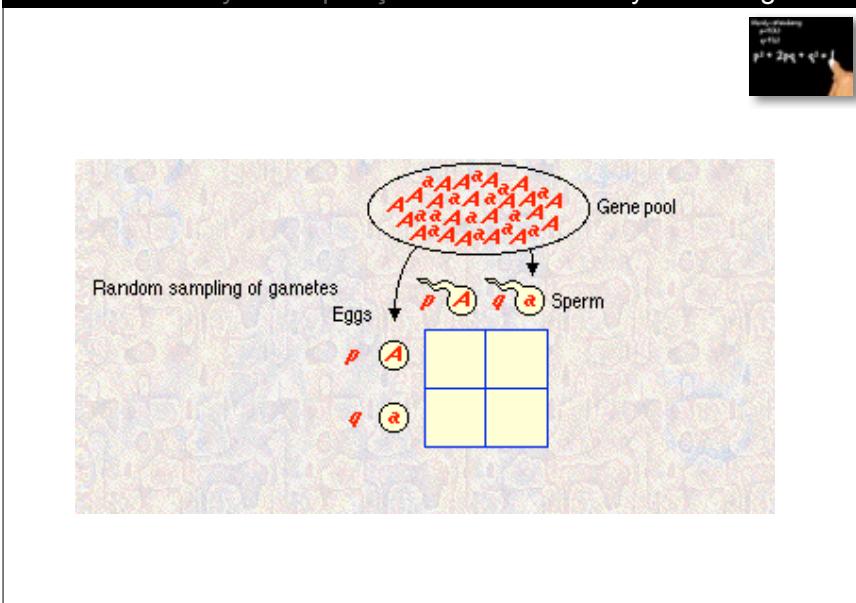
Genetic variability • Composição Genética • Hardy-Weinberg

HWE: establishes the relationship that can be used to predict **allele frequencies** given **genotype frequencies** or predict **genotype frequencies** given **allele frequencies**

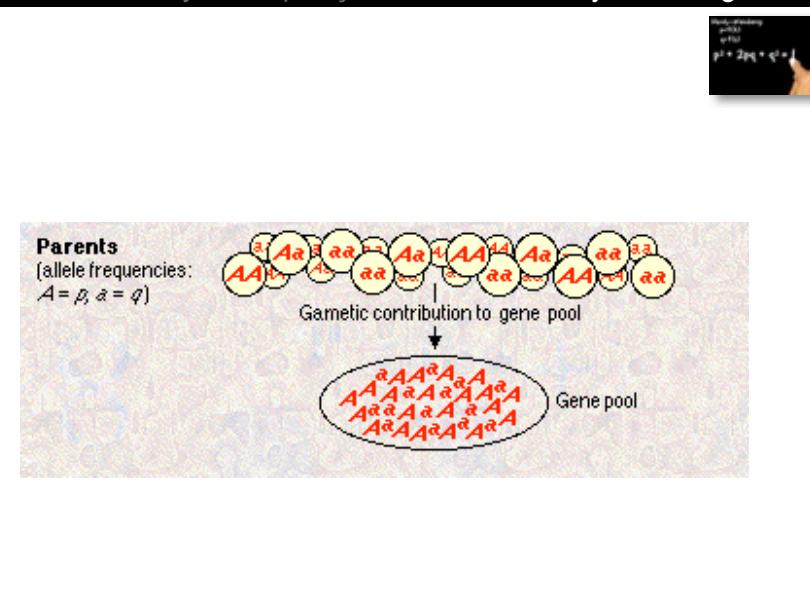
Genetic variability • Composição Genética • Hardy-Weinberg



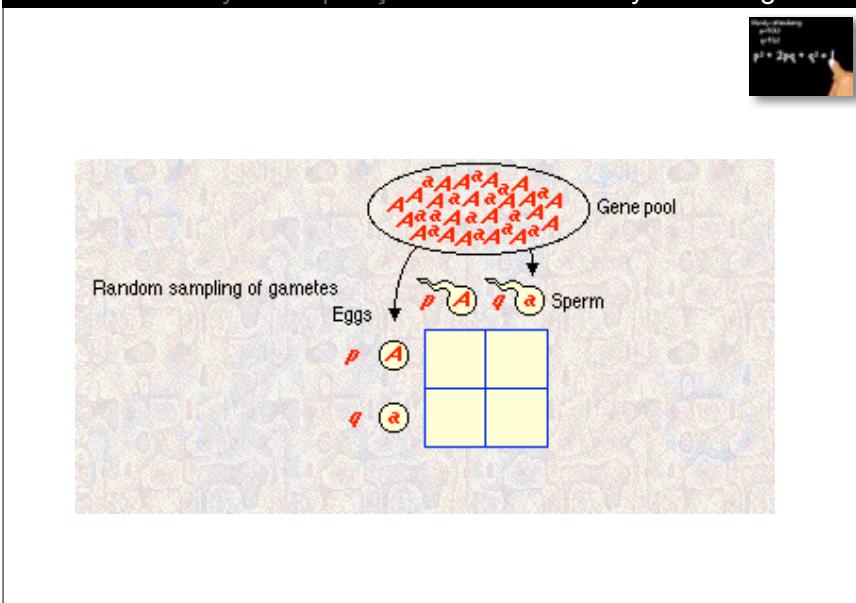
Genetic variability • Composição Genética • Hardy-Weinberg



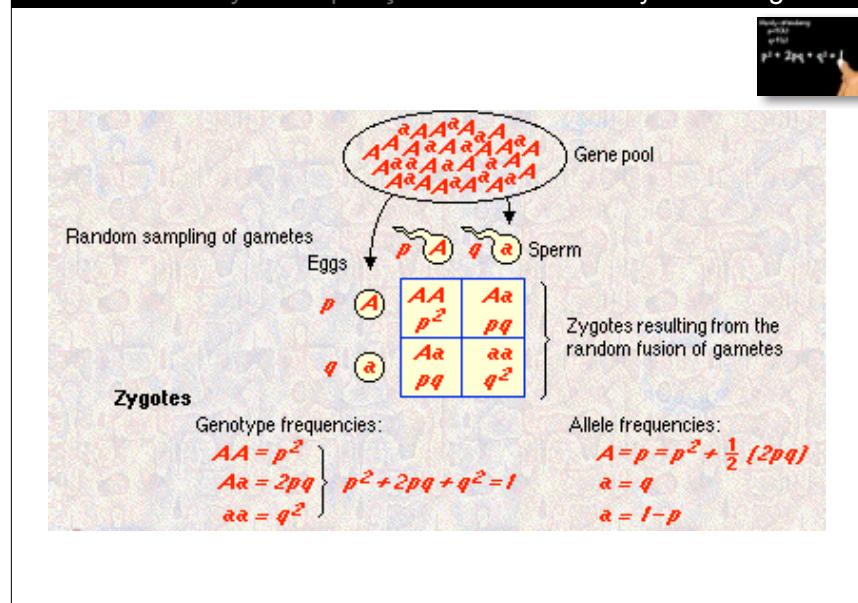
Genetic variability • Composição Genética • Hardy-Weinberg



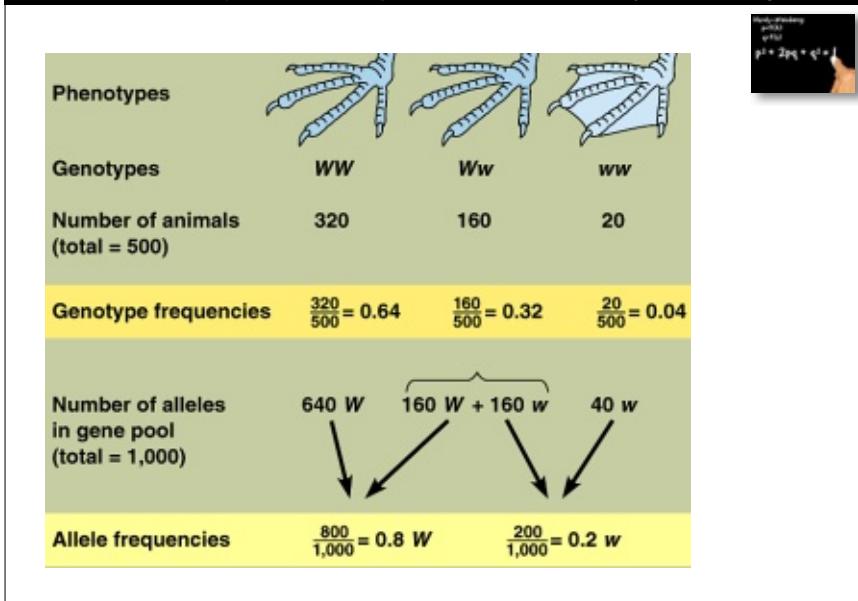
Genetic variability • Composição Genética • Hardy-Weinberg



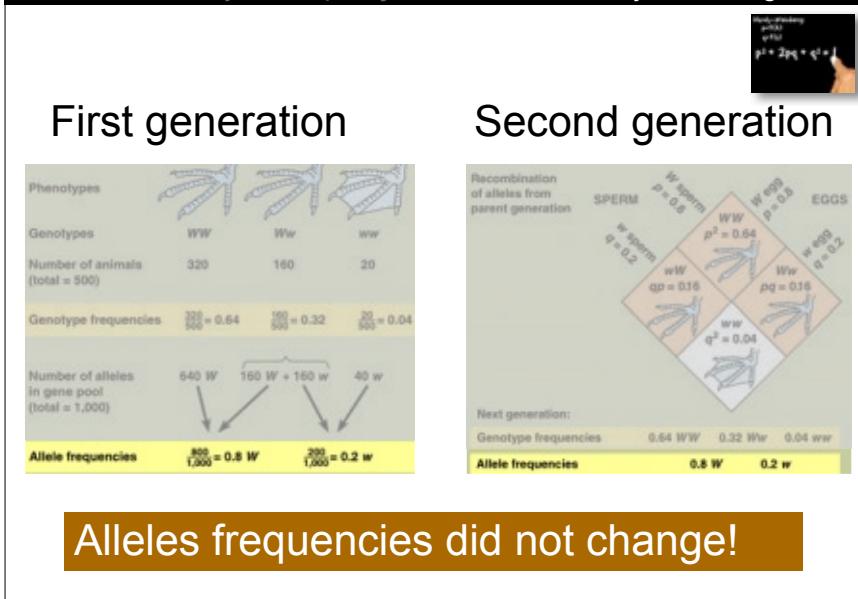
Genetic variability • Composição Genética • Hardy-Weinberg



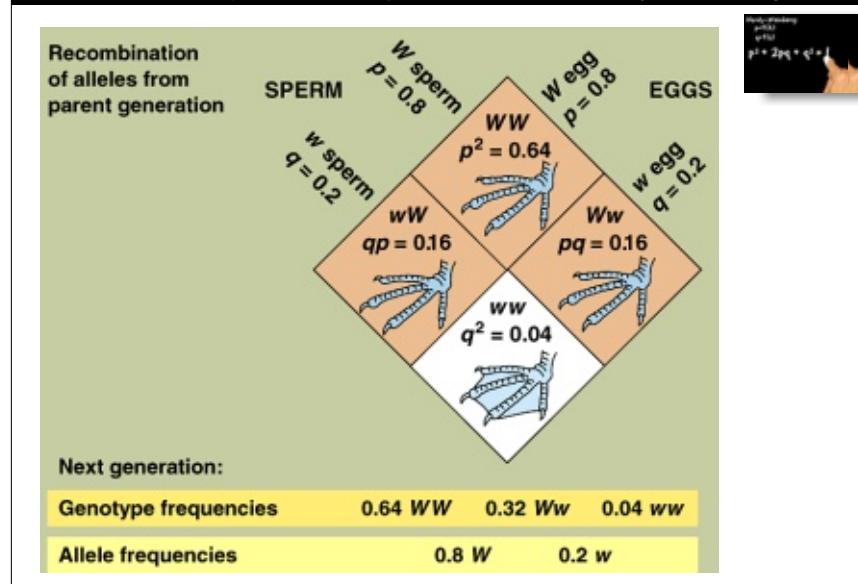
Genetic variability • Composição Genética • Hardy-Weinberg



Genetic variability • Composição Genética • Hardy-Weinberg



Genetic variability • Composição Genética • Hardy-Weinberg



Genetic variability • Composição Genética • Hardy-Weinberg

A single generation of reproduction where a set of conditions, or assumptions, are met will result in a population that meets Hardy-Weinberg expected genotype frequencies

$$p^2 + 2pq + q^2 = 1$$

Se p e q forem as frequências alélicas de A e B numa geração, as frequências genotípicas na geração seguinte serão:

p^2	q^2	$2pq$
$f(AA)$	$f(BB)$	$f(AB)$

[expansão do binómio $(p+q)^2$]

$$p^2 + 2pq + q^2 = 1$$

• População modelo?

A reprodução é sexual, envolve gâmetas de tipos distintos, mas cuja contribuição em termos de sexos é igual (isto é a frequência de um alelo é igual nos dois sexos);

As gerações não se sobrepõem;

Os cruzamentos são casuais;

A população é de grandes dimensões;

A migração é negligível;

Não há mutação;

A selecção natural não afecta os alelos em questão.

$$p^2 + 2pq + q^2 = 1$$

Para uma população com 3 alelos temos que a relação entre os dois tipos de frequências é descrita pelo polinómio: $(p+q+r)^2$:

AA p^2	AC $2pq$	CC q^2	BB r^2	AB $2pr$	CB $2qr$
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$$p^2 + 2pq + q^2 = 1$$

$$p^2 + 2pq + q^2 = 1$$

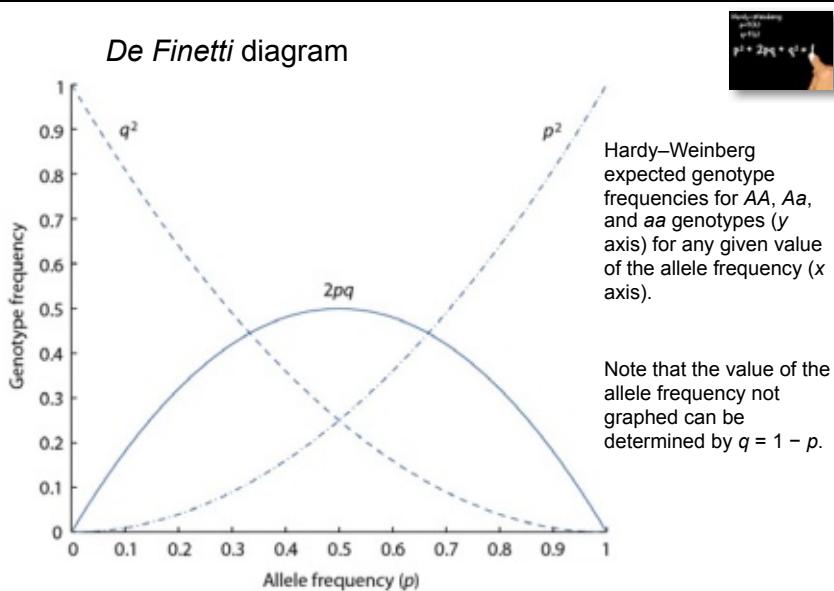
Pressupostos	Razão
População grande	Muitas possibilidades de combinações alélicas
Sem selecção natural	Não há restrição nos cruzamentos pelo que todos os alelos têm igual probabilidade de integrar a geração seguinte
Sem mutação	Não há introdução de novos alelos
Sem migração	Não há entrada ou saída de indivíduos
Cruzamentos ao acaso	Qualquer combinação de alelos é igualmente provável.

Nenhum destes pressupostos é realista....

IMPORTANTE

Descreve a relação, numa população modelo, entre as frequências alélicas numa geração e as frequências genotípicas da geração seguinte: sendo $f(A)$ e $f(B)$ numa geração, as frequências genotípicas da geração seguinte serão

$$f(AA) = f(A)^2; f(AB) = 2 f(A) f(B) \text{ e } f(BB) = f(B)^2$$

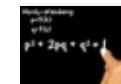
*De Finetti diagram***IMPORTANTE**

Descreve a relação, numa população modelo, entre as frequências alélicas numa geração e as frequências genotípicas da geração seguinte: sendo $f(A)$ e $f(B)$ numa geração, as frequências genotípicas da geração seguinte serão

$$f(AA) = f(A)^2; f(AB) = 2 f(A) f(B) \text{ e } f(BB) = f(B)^2$$

As frequências alélicas entre gerações não se alteram.

Esta relação estabelece-se de uma geração para a seguinte e perdura enquanto as condições da população modelo se mantiverem.



What good is a model with so many restrictive assumptions?
Are all these assumptions likely to be met in actual populations?

$$\begin{array}{l} \text{Hardy-Weinberg} \\ p^2 + 2pq + q^2 = 1 \end{array}$$

The Hardy–Weinberg model is not necessarily meant to be an exact description of any actual population...

although actual populations often exhibit genotype frequencies predicted by Hardy– Weinberg

$$\begin{array}{l} \text{Hardy-Weinberg} \\ p^2 + 2pq + q^2 = 1 \end{array}$$

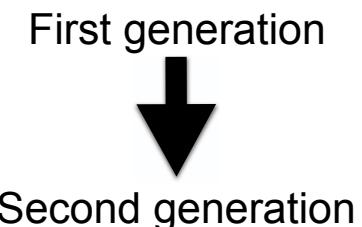
- X Mutation
- X Drift
- X Selection
- X Migration

$$\begin{array}{l} \text{Hardy-Weinberg} \\ p^2 + 2pq + q^2 = 1 \end{array}$$

So....

$$\begin{array}{l} \text{Hardy-Weinberg} \\ p^2 + 2pq + q^2 = 1 \end{array}$$

- X Mutation
- X Drift
- X Selection
- X Migration

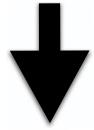


Alleles frequencies did not change!

$$\begin{array}{l} \text{Hardy-Weinberg} \\ p^2 + 2pq + q^2 = 1 \\ p^2 + 2pq + q^2 = 1 \end{array}$$

Alleles frequencies did not change!

First generation



Second generation

$$\begin{array}{l} \text{Hardy-Weinberg} \\ p^2 + 2pq + q^2 = 1 \\ p^2 + 2pq + q^2 = 1 \end{array}$$

Alleles frequencies did not change!

First generation



Second generation

? Mutation

? Drift

? Selection

? Migration

$$\begin{array}{l} \text{Hardy-Weinberg} \\ p^2 + 2pq + q^2 = 1 \\ p^2 + 2pq + q^2 = 1 \end{array}$$

Phenotypes			
Genotypes	BB	Bb	bb
Number of Individuals (total = 100)	49	42	9
Genotype Frequencies	49/100 = 0.49	42/100 = 0.42	9/100 = 0.09
Alleles contributed to Gene Pool (total = 200)	98 B	42 B 42 b	18 b
Allele Frequencies	for allele B, (98+42)/200 = 0.7		For allele b, (42+18)/200 = 0.3

$$\begin{array}{l} \text{Hardy-Weinberg} \\ p^2 + 2pq + q^2 = 1 \\ p^2 + 2pq + q^2 = 1 \end{array}$$

Punnett square

Probability of Alleles in Gametes: Sperm and Eggs	0.7 B		0.3 b
	0.7 B	0.3 b	0.3 b
0.7 B	BB 0.7 X 0.7 = 0.49	Bb 0.7 X 0.3 = 0.21	Bb 0.7 X 0.3 = 0.21
0.3 b	Bb 0.7 X 0.3 = 0.21	bb 0.3 X 0.3 = 0.09	bb 0.3 X 0.3 = 0.09

Genetic variability • Composição Genética • Hardy-Weinberg

$$\begin{array}{l} \text{Hardy-Weinberg} \\ p^2 + 2pq + q^2 = 1 \end{array}$$

A	BB	Bb	bb
<i>Genotype Frequencies in Next Generation</i>	0.49	0.21+0.21=0.42	0.09

Genetic variability • Composição Genética • Hardy-Weinberg

$$\begin{array}{l} \text{Hardy-Weinberg} \\ p^2 + 2pq + q^2 = 1 \end{array}$$

	BB	Bb	bb
<i>Genotype Frequencies in Next Generation</i>	0.49	0.21+0.21=0.42	0.09
<i>Allele Frequencies in Next Generation</i>	B	b	
	$0.49 + 0.49 + 0.42 = 1.40/2 = 0.7$	$0.42 + 0.09 + 0.09 = 0.60/2 = 0.3$	

Genetic variability • Composição Genética • Hardy-Weinberg

$$\begin{array}{l} \text{Hardy-Weinberg} \\ p^2 + 2pq + q^2 = 1 \end{array}$$

	BB	Bb	bb
<i>Genotype Frequencies in Next Generation</i>	0.49	0.21+0.21=0.42	0.09
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	BB	Bb	bb
<i>Genotype Frequencies in Next Generation</i>	0.49	0.21+0.21=0.42	0.09
<i>Allele Frequencies in Next Generation</i>	$0.49 + 0.49 + 0.42 = 1.40/2 = 0.7$	$0.42 + 0.09 + 0.09 = 0.60/2 = 0.3$	

Initial frequencies

Allele Frequencies	for allele B , $(98+42)/200 = 0.7$		For allele b , $(42+18)/200 = 0.3$

EXAMPLES

Does Hardy-Weinberg equilibrium ever exist in nature?

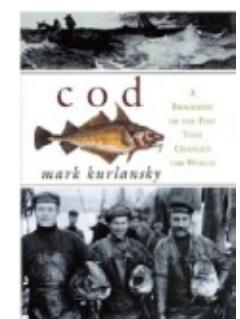
Example: Atlantic cod (*Gadus morhua*) in Nova Scotia



as a juvenile...



... and as an adult



EXAMPLES

Does Hardy-Weinberg equilibrium ever exist in nature?

Example: Atlantic cod (*Gadus morhua*) in Nova Scotia

A sample of 364 fish were scored for a single nucleotide locus

$$A_1A_1 = 109$$

$$A_1A_2 = 182$$

$$A_2A_2 = 73$$

EXAMPLES

$$A_1A_1 = 109$$

$$A_1A_2 = 182$$

$$A_2A_2 = 73$$

$$\text{Total: } 109+182+73=364$$

Passo 1: Calculem as frequências genotípicas

Frequência de A_1A_1

Frequência de A_1A_2

Frequência de A_2A_2

EXAMPLES

$$A_1A_1 = 109$$

$$A_1A_2 = 182$$

$$A_2A_2 = 73$$

Passo 1: Calculem as frequências genotípicas

$$\text{Frequency de } A_1A_1 = 109/364 = 0.2995$$

$$\text{Frequency de } A_1A_2 = 182/364 = 0.5000$$

$$\text{Frequency de } A_2A_2 = 73/364 = 0.2005$$

$$\begin{aligned}f(A_1A_1) &= 0.2995 \\f(A_1A_2) &= 0.5000 \\f(A_2A_2) &= 0.2005\end{aligned}$$

EXAMPLES

$$f(A_1A_1) = 0.2995$$

$$f(A_1A_2) = 0.5000$$

$$f(A_2A_2) = 0.2005$$

Passo 2: Calculem as frequências alélicas

Frequency de A_1

Frequency de A_2

EXAMPLES

$$\begin{aligned}f(A_1A_1) &= 0.2995 \\f(A_1A_2) &= 0.5000 \\f(A_2A_2) &= 0.2005\end{aligned}$$

Passo 2: Calculem as frequências alélicas

$$\text{Frequency of } A_1 = p = \text{Freq}(A_1A_1) + \frac{1}{2} \text{ Freq}(A_1A_2)$$

$$\text{Frequency of } A_2 = q = \text{Freq}(A_2A_2) + \frac{1}{2} \text{ Freq}(A_1A_2)$$

EXAMPLES

$$\begin{aligned}f(A_1A_1) &= 0.2995 \\f(A_1A_2) &= 0.5000 \\f(A_2A_2) &= 0.2005\end{aligned}$$

Passo 2: Calculem as frequências alélicas

$$\begin{aligned}\text{Frequency of } A_1 = p &= \text{Freq}(A_1A_1) + \frac{1}{2} \text{ Freq}(A_1A_2) \\&= 0.2995 + \frac{1}{2} (0.5000) \\&= 0.5495\end{aligned}$$

EXAMPLES

$$\begin{aligned}f(A_1A_1) &= 0.2995 \\f(A_1A_2) &= 0.5000 \\f(A_2A_2) &= 0.2005\end{aligned}$$

Passo 2: Calculem as frequências alélicas

$$\begin{aligned}\text{Frequency of } A_1 = p &= \text{Freq}(A_1A_1) + \frac{1}{2} \text{ Freq}(A_1A_2) \\&= 0.2995 + \frac{1}{2} (0.5000) \\&= 0.5495\end{aligned}$$

$$\begin{aligned}\text{Frequency of } A_2 = q &= \text{Freq}(A_2A_2) + \frac{1}{2} \text{ Freq}(A_1A_2) \\&= 0.2005 + \frac{1}{2} (0.5000) \\&= 0.4505\end{aligned}$$

Check that $p + q = 0.5495 + 0.4505 = 1$

EXAMPLES

$$\begin{aligned}f(A_1) &= 0.5495 \\f(A_2) &= 0.4505\end{aligned}$$

Passo 3: Estimar as frequências genotípicas em EHW

$$\text{Expected No. of } A_1A_1 = p^2 \times N$$

$$\text{Expected No. of } A_1A_2 = 2pq \times N$$

$$\text{Expected No. of } A_2A_2 = q^2 \times N$$

EXAMPLES

$$f(A_1) = 0.5495$$

$$f(A_2) = 0.4505$$

Passo 3: Estimar as frequências genotípicas em EHW

$$\text{Expected No. of } A_1A_1 = p^2 \times N$$

$$= (0.5495)^2 \times 364$$

$$= 109.9$$

$$\text{Expected No. of } A_1A_2 = 2pq \times N$$

$$= 2(0.5495)(0.4505) \times 364$$

$$= 180.2$$

$$\text{Expected No. of } A_2A_2 = q^2 \times N$$

$$= (0.4505)^2 \times 364$$

$$= 73.9$$

EXAMPLES

$$Nb_0(A_1A_1) = 109$$

$$Nb_0(A_1A_2) = 182$$

$$Nb_0(A_2A_2) = 73$$

$$Nb_E(A_1A_1) = 109.9$$

$$Nb_E(A_1A_2) = 180.2$$

$$Nb_E(A_2A_2) = 73.9$$

Passo 4: Comparar frequências genotípicas observadas e esperadas em EHW

Genotype	Observed	Expected
A ₁ A ₁	109	109.9
A ₁ A ₂	182	180.2
A ₂ A ₂	73	73.9

EXAMPLES

$$Nb_0(A_1A_1) = 109$$

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Passo 4: Comparar frequências genotípicas observadas e esperadas em EHW

Genotype	Observed	Expected
A ₁ A ₁	109	109.9
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A ₂ A ₂	73	73.9

$$\chi^2_{\text{calc}} = \sum \frac{(Obs. - Exp.)^2}{Exp.} = 0.036$$

Graus de liberdade = número de classes (AA, AB, BB) - 1 - número de parâmetros estimados (p,q)= 1

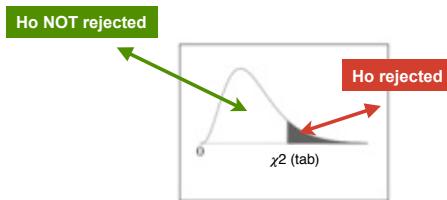
EXAMPLES

Hipótese nula H₀:

as proporções genotípicas observadas não diferem das proporções esperadas de acordo com a lei de HW

EXAMPLES

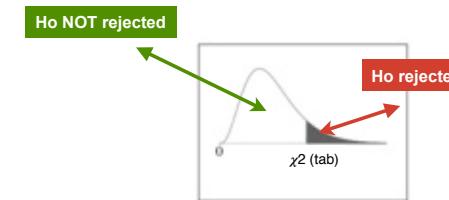
χ^2 e probabilidade



df	$\chi^2_{.995}$	$\chi^2_{.990}$	$\chi^2_{.975}$	$\chi^2_{.950}$	$\chi^2_{.900}$	$\chi^2_{.100}$	$\chi^2_{.050}$	$\chi^2_{.025}$	$\chi^2_{.010}$	$\chi^2_{.005}$
1	0.000	0.000	0.001	0.004	0.016	2.706	3.841	5.024	6.635	7.879
2	0.010	0.020	0.051	0.103	0.211	4.605	5.991	7.378	9.210	10.597
3	0.072	0.115	0.216	0.352	0.584	6.251	7.815	9.348	11.345	12.838
4	0.207	0.297	0.484	0.711	1.064	7.779	9.488	11.143	13.277	14.860
5	0.412	0.554	0.831	1.145	1.610	9.236	11.070	12.833	15.086	16.750
6	0.676	0.872	1.237	1.635	2.204	10.645	12.592	14.449	16.812	18.548
7	0.989	1.239	1.690	2.167	2.833	12.017	14.067	16.013	18.475	20.278
8	1.344	1.646	2.180	2.733	3.490	13.362	15.507	17.535	20.090	21.955

EXAMPLES

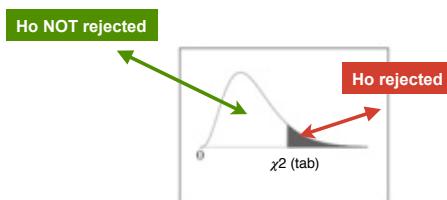
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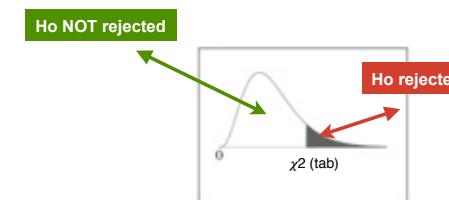
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EXAMPLES

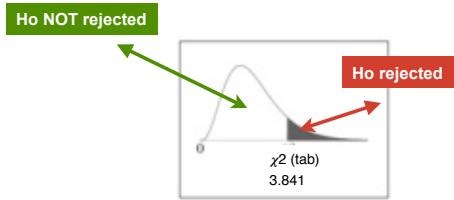
χ^2 e probabilidade



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EXAMPLES

Conclusion ??



$\chi^2_{\text{calc}} < \chi^2_{\text{tab}}$ = null hypothesis NOT rejected

$\chi^2_{\text{calc}} > \chi^2_{\text{tab}}$ = null hypothesis rejected

Genetic variability • Composição Genética • Hardy-Weinberg



Genetic variability • Composição Genética • Hardy-Weinberg



$$AA = 320$$

$$AB = 570$$

$$BB = 320$$

$$\text{SUM} = 1210$$

Genetic variability • Composição Genética • Hardy-Weinberg



$$AA = 320$$

$$AB = 570$$

$$BB = 320$$

$$\text{SUM} = 1210$$

$$f(AA) = 320/1210$$

$$f(AB) = 570/1210$$

$$f(BB) = 320/1210$$

Genetic variability • Composição Genética • Hardy-Weinberg

$$p^2 + 2pq + q^2 = 1$$

$$AA = 320$$

$$AB = 570$$

$$BB = 320$$

$$SUM= 1210$$

$$f(AA) = 150/800$$

$$f(AB) = 500/800$$

$$f(BB) = 150/800$$

$$f(AA) = 0.25$$

$$f(AB) = 0.50$$

$$f(BB) = 0.25$$

Genetic variability • Composição Genética • Hardy-Weinberg

$$p^2 + 2pq + q^2 = 1$$

$$f(AA) = 0.25 \quad f(A) =$$

$$f(AB) = 0.50 \quad f(B) =$$

$$f(BB) = 0.25$$

Genetic variability • Composição Genética • Hardy-Weinberg

$$p^2 + 2pq + q^2 = 1$$

$$f(AA) = 0.25$$

$$f(AB) = 0.50$$

$$f(BB) = 0.25$$

$$f(A) = (320+570/2)/1210$$

Contagem de indivíduos

$$f(B) = (640+570)/2420$$

Contagem de alelos

$$f(A) = 0.25+0.50/2 = 0.50$$

A partir das frequências

$$f(B) = 0.25+0.50/2 = 0.50$$

Genetic variability • Composição Genética • Hardy-Weinberg

$$p^2 + 2pq + q^2 = 1$$

$$f(AA) = 0.1875$$

$$f(AB) = 0.625$$

$$f(BB) = 0.188$$

$$f(A) = 0.5$$

$$f(B) = 0.5$$

Genetic variability • Composição Genética • Hardy-Weinberg

$$\begin{array}{ll} f(AA) = 0.25 & f(A) = 0.5 \\ f(AB) = 0.50 & f(B) = 0.5 \\ f(BB) = 0.25 & \end{array}$$

$p^2 + 2pq + q^2 = 1$

$p + q = 1$

	Obs	Esp
AA	320	$0.5^2 * 1210 = 302.5$
AB	570	$2 * 0.5 * 0.5 * 1210 = 605$
BB	320	$0.5^2 * 1210 = 302.5$

Genetic variability • Composição Genética • Hardy-Weinberg

	Obs	Esp
AA	150	$0.5^2 * 800 = 200$
AB	500	$2 * 0.5 * 0.5 * 800 = 400$
BB	150	$0.5^2 * 800 = 200$

$$\chi^2 (\text{calc}) = 4.050$$

$$\chi^2 (\text{tab}) = 3.841$$

Conclusion?

Genetic variability • Composição Genética • Hardy-Weinberg

	Obs	Esp
AA	320	$0.5^2 * 1210 = 302.5$
AB	570	$2 * 0.5 * 0.5 * 1210 = 605$
BB	320	$0.5^2 * 1210 = 302.5$

$$\chi^2 = \sum \frac{(\text{Obs.} - \text{Exp.})^2}{\text{Exp.}}$$

$$\begin{aligned} \chi^2 &= \sum \frac{(320 - 302.5)^2}{302.5} + \frac{(570 - 605)^2}{605} + \frac{(320 - 302.5)^2}{302.5} \\ &= 1.012 + 2.025 + 1.012 = 4.05 \end{aligned}$$

EXAMPLES



EXAMPLES

A terrible crime has been committed.

Left at the crime scene was:

a *biological sample*

that law-enforcement authorities used to obtain a *multilocus genotype* or DNA profile.

EXAMPLES



A suspect in the crime has been identified and subpoenaed to provide a tissue sample for DNA profiling.

EXAMPLES

Section of victim's DNA:



There are three regions of repetitive DNA.

Section of suspect's DNA:



The same three regions of repetitive DNA are present here, but some include different numbers of repeats. Now let's compare this sample to...

Section of DNA from crime scene hair:



The lengths of the repetitive sequences match the lengths in the suspect's DNA — so the DNA found at the crime scene belongs to the suspect.

EXAMPLES



The DNA profiles from the suspect and from the crime scene are identical.

EXAMPLES



The DNA profiles from the suspect and from the crime scene are identical.

Can we unequivocally say the suspect is the guilty party?

EXAMPLES

Can anybody else share the same DNA profile?

Two matching profiles = same person??

EXAMPLES

Let's see....

EXAMPLES

What is the probability that two individuals share the same profile??

HW prediction will help, but....

in using HW we are implicitly accepting that all of the assumptions of Hardy-Weinberg are approximately met.

EXAMPLES

Caution:

For this estimation to be done we need to assume that human populations are in HW

EXAMPLES

The DNA profile is shown in the table below.

Locus	D3S1358	D21S11	D18S51
Genotype	17, 18	29, 30	18, 18

EXAMPLES

D3S1358	
Allele	Freq
12	0.0000
13	0.0025
14	0.1404
15	0.2463
16	0.2315
17	0.2118
18	0.1626
19	0.0049

EXAMPLES

D3S1358		D21S11	
Allele	Freq	Allele	Freq
12	0.0000	27	0.0459
13	0.0025	28	0.1658
14	0.1404	29	0.1811
15	0.2463	30	0.2321
16	0.2315	30.2	0.0383
17	0.2118	31	0.0714
18	0.1626	31.2	0.0995
19	0.0049	32	0.0153
		32.2	0.1122
		33.2	0.0306
		35.2	0.0026

EXAMPLES

D3S1358		D21S11		D18S51	
Allele	Freq	Allele	Freq	Allele	Freq
12	0.0000	27	0.0459	<11	0.0128
13	0.0025	28	0.1658	11	0.0128
14	0.1404	29	0.1811	12	0.1276
15	0.2463	30	0.2321	13	0.1224
16	0.2315	30.2	0.0383	14	0.1735
17	0.2118	31	0.0714	15	0.1276
18	0.1626	31.2	0.0995	16	0.1071
19	0.0049	32	0.0153	17	0.1556
		32.2	0.1122	18	0.0918
		33.2	0.0306	19	0.0357
		35.2	0.0026	20	0.0255
				21	0.0051
				22	0.0026

EXAMPLES

D3S1358	D21S11
17-allele frequency = 0.2118	29-allele frequency = 0.1811
18-allele frequency = 0.1626	30-allele frequency = 0.2321
Genotype frequency = $2(0.2118)(0.1626) = 0.0689$ or 6.89%	Genotype frequency = $2(0.1811)(0.2321) = 0.0841$ or 8.41%
D18S51	
18-allele frequency = 0.0918	
Genotype frequency = $0.0918^2 = 0.0084$ or 0.84%	
	D3S1358 = 0.0689 or 6.89%
	D21S11 = 0.0841 or 8.41%
	D18S51 = 0.0084 or 0.84%

EXAMPLES

Product rule = the probability of observing multiple independent events is just the product of each individual event

EXAMPLES

$$\begin{aligned} \text{D3S1358} &= 0.0689 \\ \text{D21S11} &= 0.0841 \\ \text{D18S51} &= 0.0084 \end{aligned}$$

$$0.0689 \times 0.0841 \times 0.0084 = 0.000049 \text{ or } 0.0049\%$$

$$\begin{aligned} 0.0049 - 100 \\ 1 - x \\ x = 100/0.0049 \end{aligned}$$

$$1/0.000049 = 20,408$$

EXAMPLES

1 in 20,408

Portugal $\approx 10^6$ people

Probability of 500 individuals will share this genotype

NOT A RARE GENOTYPE!

Genetic variability • Composição Genética • Hardy-Weinberg


$$p^2 + 2pq + q^2 = 1$$

Se uma população não se encontra em EHW, então quais as razões:

- Seleção?**
- Migração?**
- Subdivisão?**
- Deriva genética?**
- Mutação?**

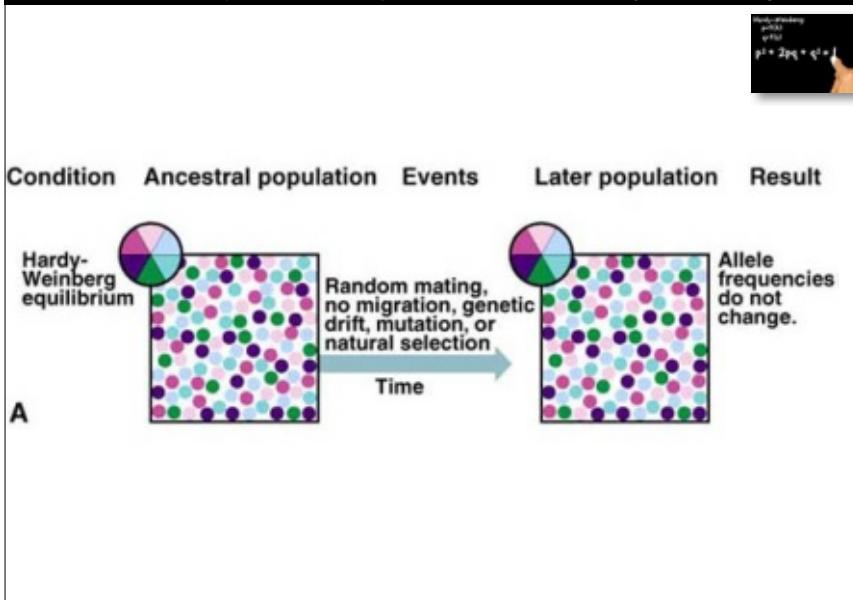
EXAMPLES

Only when DNA profiles do not match, called an “*exclusion*,” can a suspect be unambiguously and absolutely excluded as the source of a biological sample at a crime scene

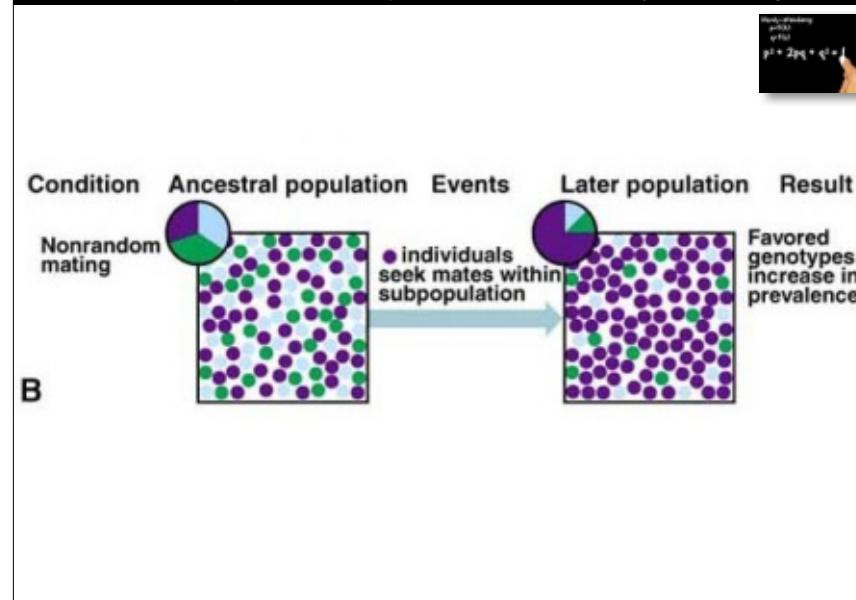
Genetic variability • Composição Genética • Hardy-Weinberg


$$p^2 + 2pq + q^2 = 1$$

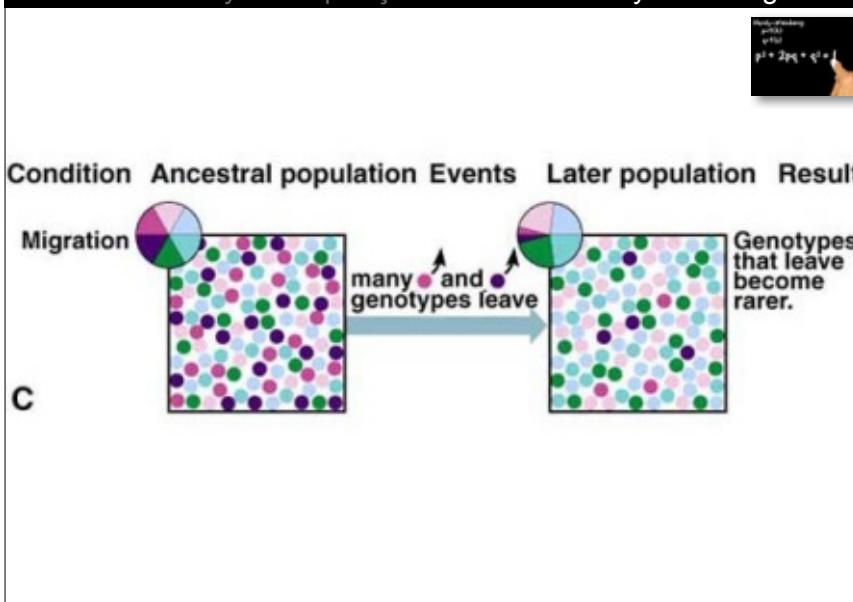
Genetic variability • Composição Genética • Hardy-Weinberg



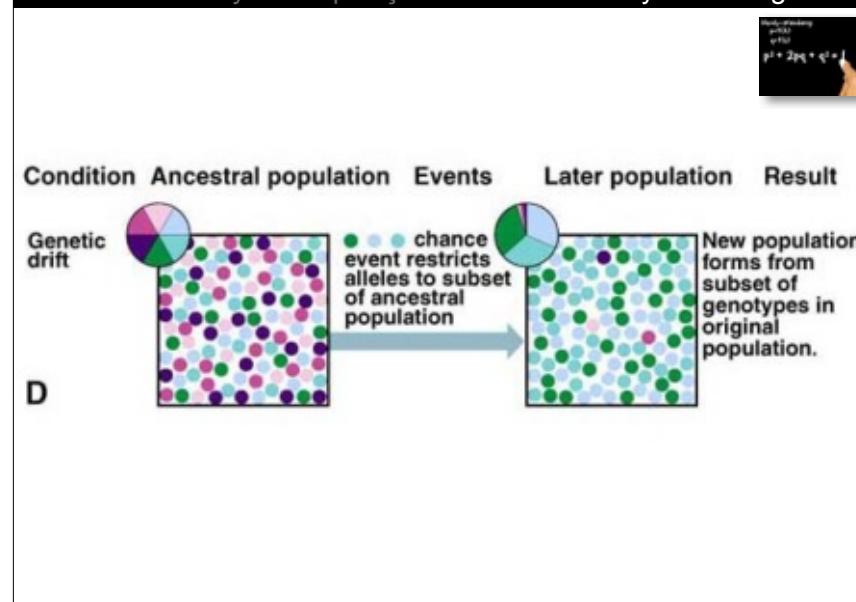
Genetic variability • Composição Genética • Hardy-Weinberg



Genetic variability • Composição Genética • Hardy-Weinberg



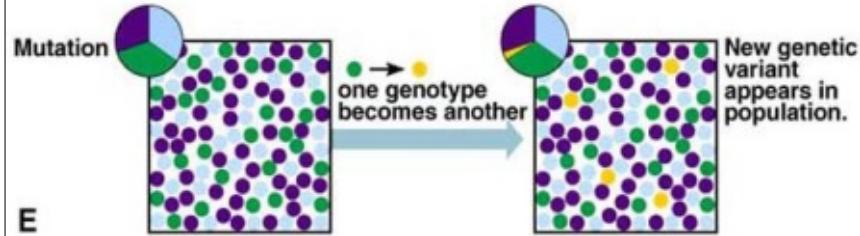
Genetic variability • Composição Genética • Hardy-Weinberg



Genetic variability • Composição Genética • Hardy-Weinberg

$$\begin{array}{l} \text{Hardy-Weinberg} \\ p^2 + 2pq + q^2 = 1 \end{array}$$

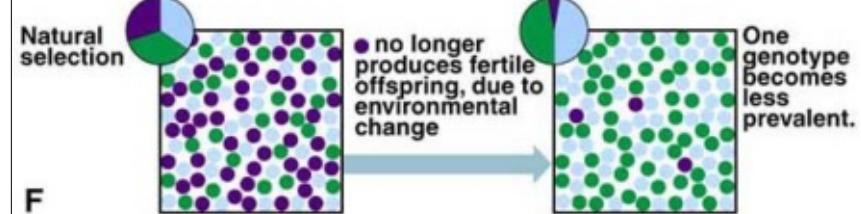
Condition Ancestral population Events Later population Result



Genetic variability • Composição Genética • Hardy-Weinberg

$$\begin{array}{l} \text{Hardy-Weinberg} \\ p^2 + 2pq + q^2 = 1 \end{array}$$

Condition Ancestral population Events Later population Result



Genetic variability • Composição Genética • Hardy-Weinberg

$$\begin{array}{l} \text{Hardy-Weinberg} \\ p^2 + 2pq + q^2 = 1 \end{array}$$

H-W is an important tool for population genetics.

If assumptions are met, we can use it to estimate allele and genotype frequencies that would otherwise be difficult to measure.

If assumptions are not met (can be tested statistically), then we know that some outside force is perturbing allele or genotype frequencies.

Genetic variability • Composição Genética • Hardy-Weinberg

$$\begin{array}{l} \text{Hardy-Weinberg} \\ p^2 + 2pq + q^2 = 1 \end{array}$$

Take-home message

The **all-important** concepts of allele frequency and genotype frequency are central to the **Hardy-Weinberg principle**, which states that in the absence of perturbing factors, allele and genotype frequencies in a bi-allelic system remain constant over generations, with genotype frequencies at a ratio of $p^2:2pq:q^2$, in which p and q represent allele frequencies.

In this class we have covered:

The Hardy-Weinberg principle

Main concepts

How to evaluate the HWE in a sample

What are the main factors that affect HWE